



POLITECNICO
MILANO 1863

A COMPUTATIONAL MODEL OF THE INTERACTION BETWEEN MICROCIRCULATION AND TISSUE INTERSTITIUM

Prediction and Modeling
of response to Molecular
and External Beam
Radiotherapies

Session 3: Methodological
aspects of *in silico*
multiparametric modeling



POLITECNICO DI MILANO

LaBS

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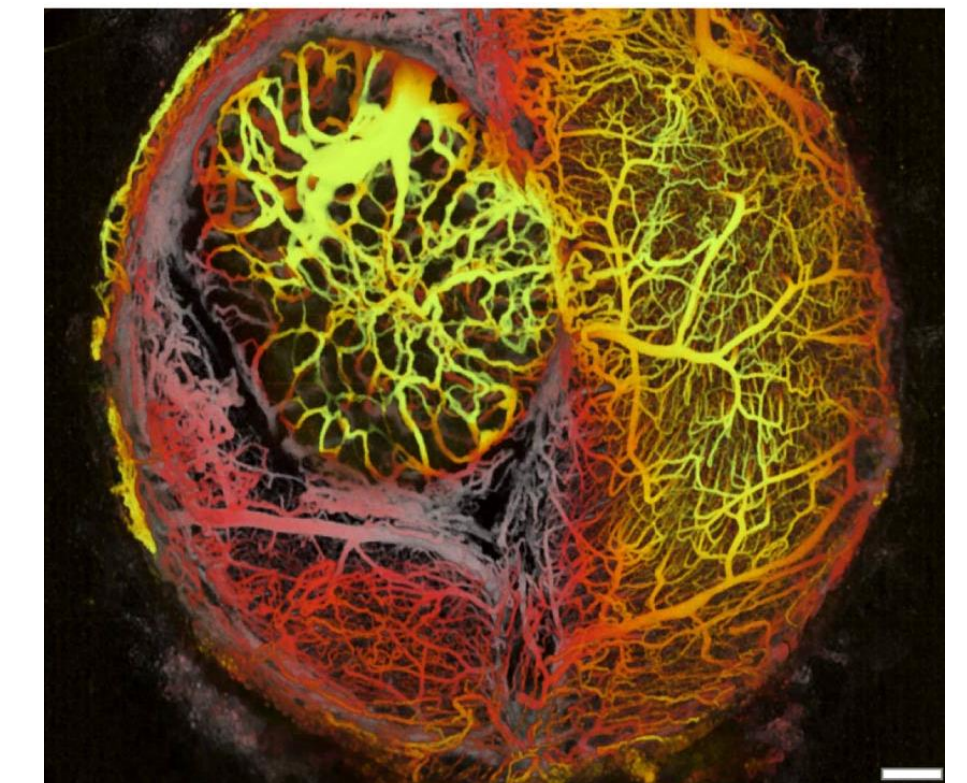
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Introduction

We present a sophisticated mathematical and computational model for coupled flow, heat and mass transport in the tumor microenvironment and we apply it to study advanced cancer treatments. Such phenomena are at the basis of the exchange of nutrients, wastes and pharmacological agents between the cardiovascular system and the organs. They are particularly interesting for the study of effective therapies to treat vascularized tumors. We develop a model applicable at the microscopic scale, where the capillaries and the interstitial volume can be described as independent structures capable to propagate flow and chemicals.



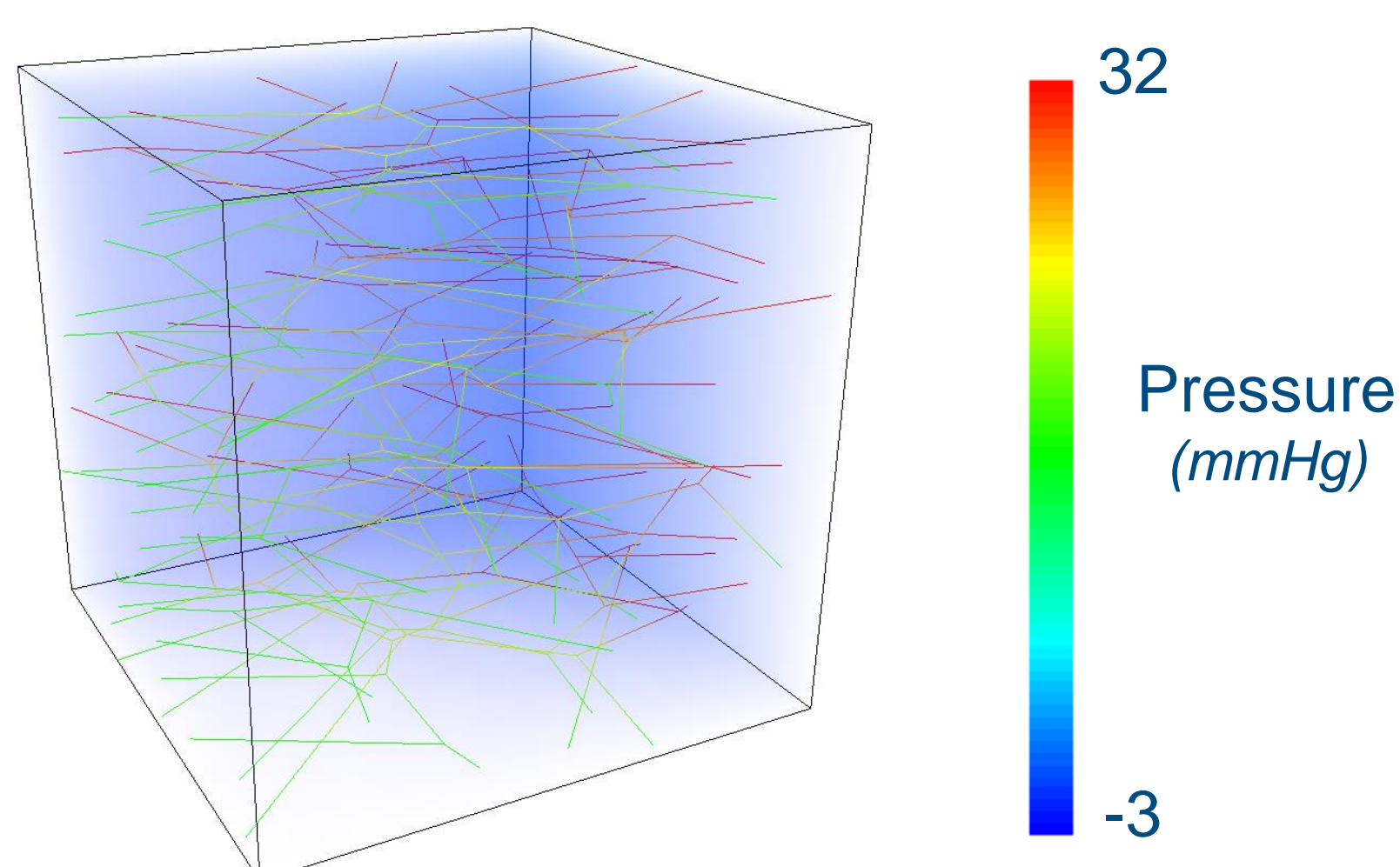
from: steelclabs.mgh.harvard.edu



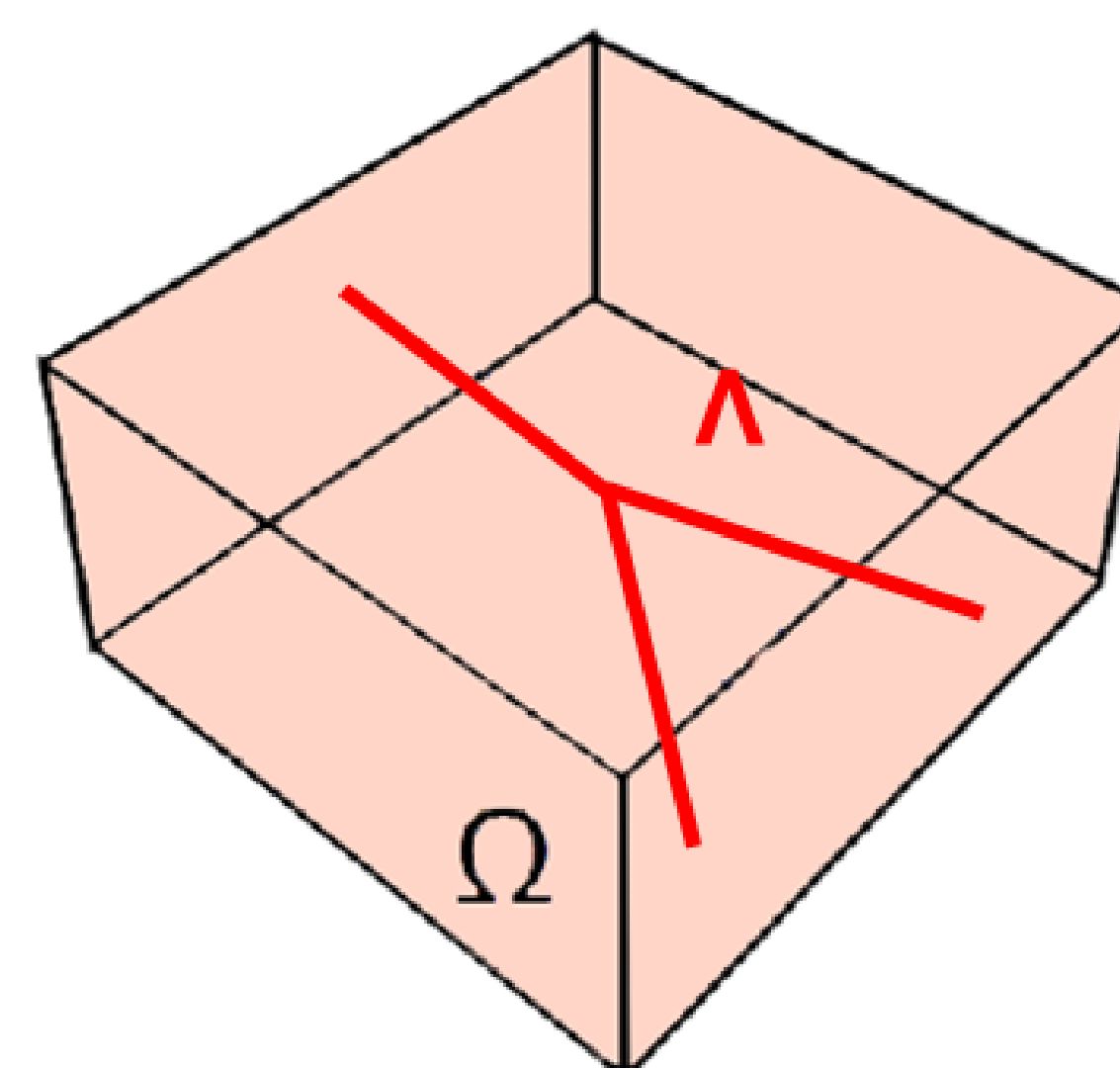
Model

The model has the unique ability of combining the following features: (i) realistic vasculature; (ii) coupled capillary and interstitial flow; (iii) hematocrit dependent flow properties (Fåhræus-Lindqvist effect); (iv) prediction of red blood cells distribution along the vasculature (with plasma skimming effect); (v) coupled capillary and interstitial mass transfer applied to nanoparticles; and (vi) coupled capillary and interstitial heat transfer.

Realistic vasculature (soon including curvature of vessels)



Coupled capillary and interstitial flow



Porous media for Ω
(Darcy's law)

Cylindrical conduits for Λ
(Poiseuille's law)

Lymphatic drainage included
(non-linear function of fluid pressure)

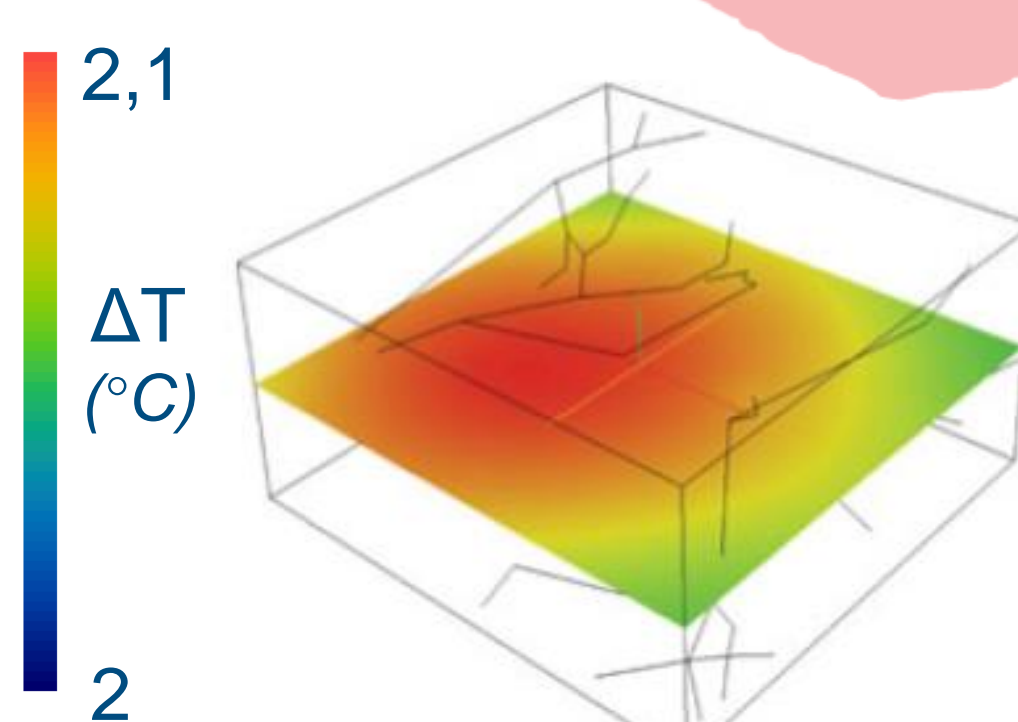
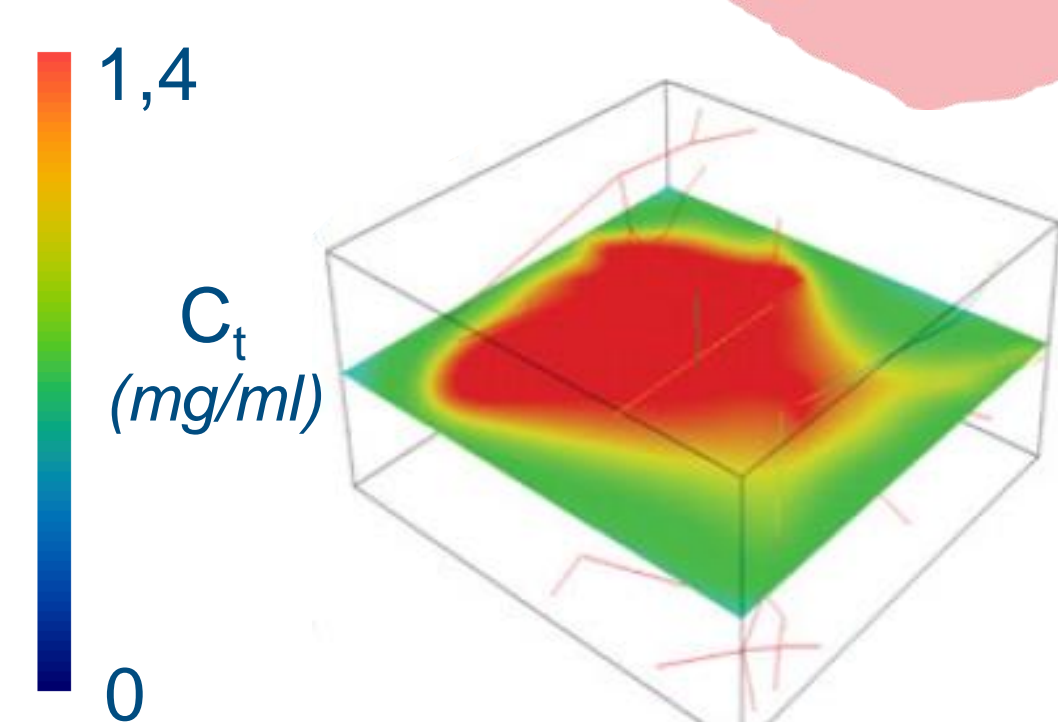
Leakage across capillary wall
(Starling's equation)

Coupled capillary and interstitial heat transfer

Particles release

Heating using alternating
magnetic field

AMF

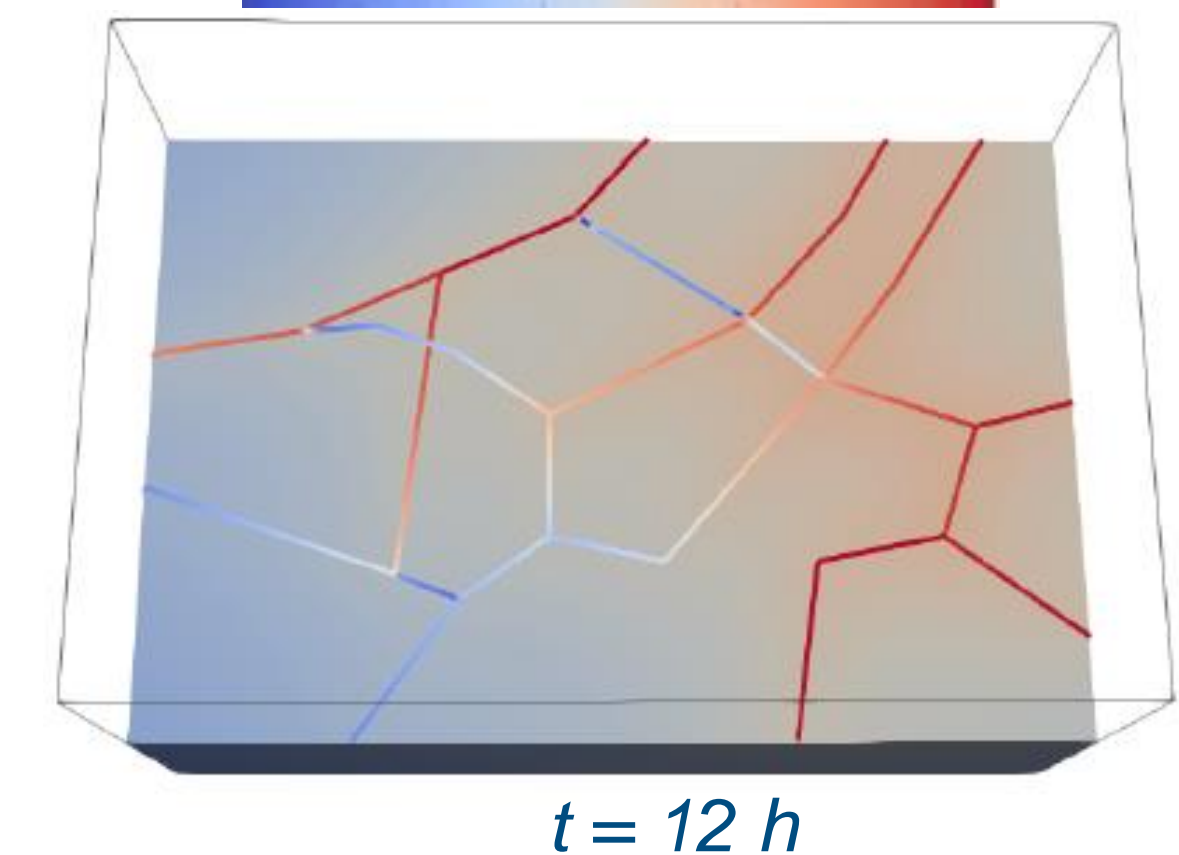
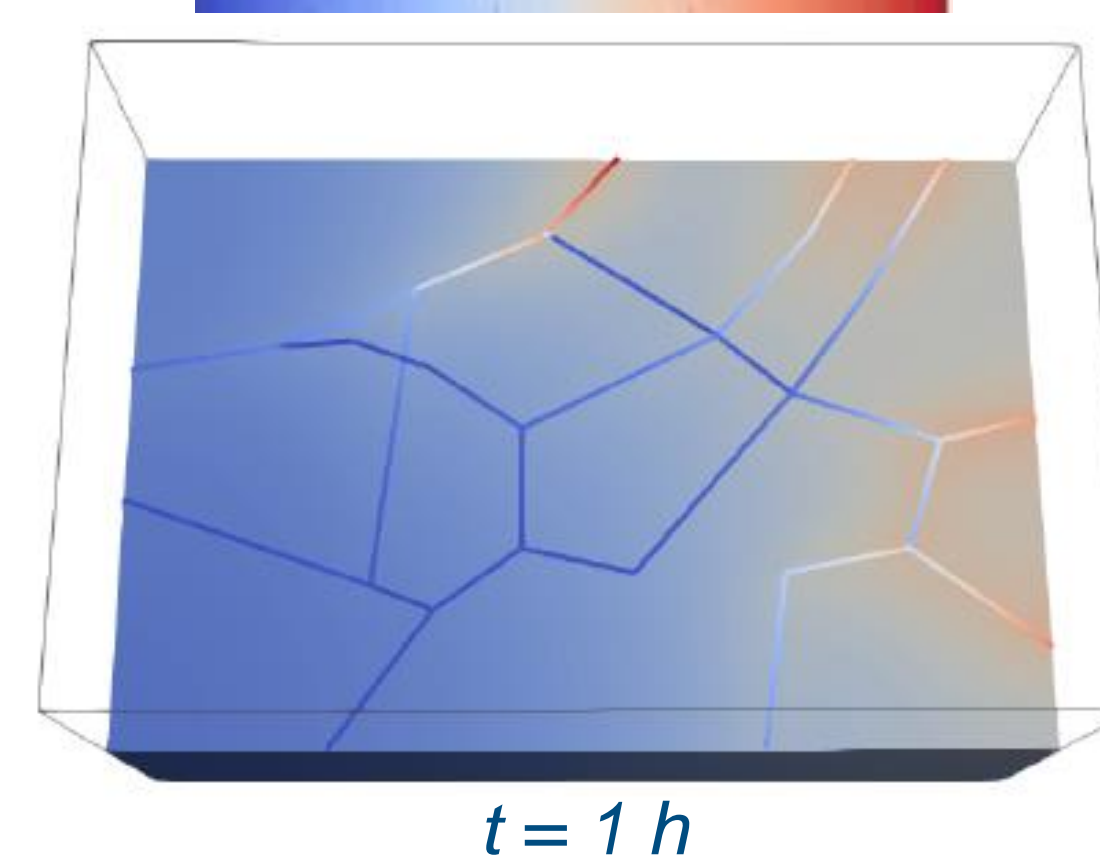


adapted from: Nabil, Decuzzi, Zunino (2015)

Coupled capillary and interstitial mass transfer for nanoparticles

Nanoparticle density on
vessel wall (m^2) 0 3
[Dextran] $_{\Omega}$ (ng/m^3) 0 0.7

Nanoparticle density on
vessel wall (m^2) 0 7
[Dextran] $_{\Omega}$ (ng/m^3) 1.4 1.6

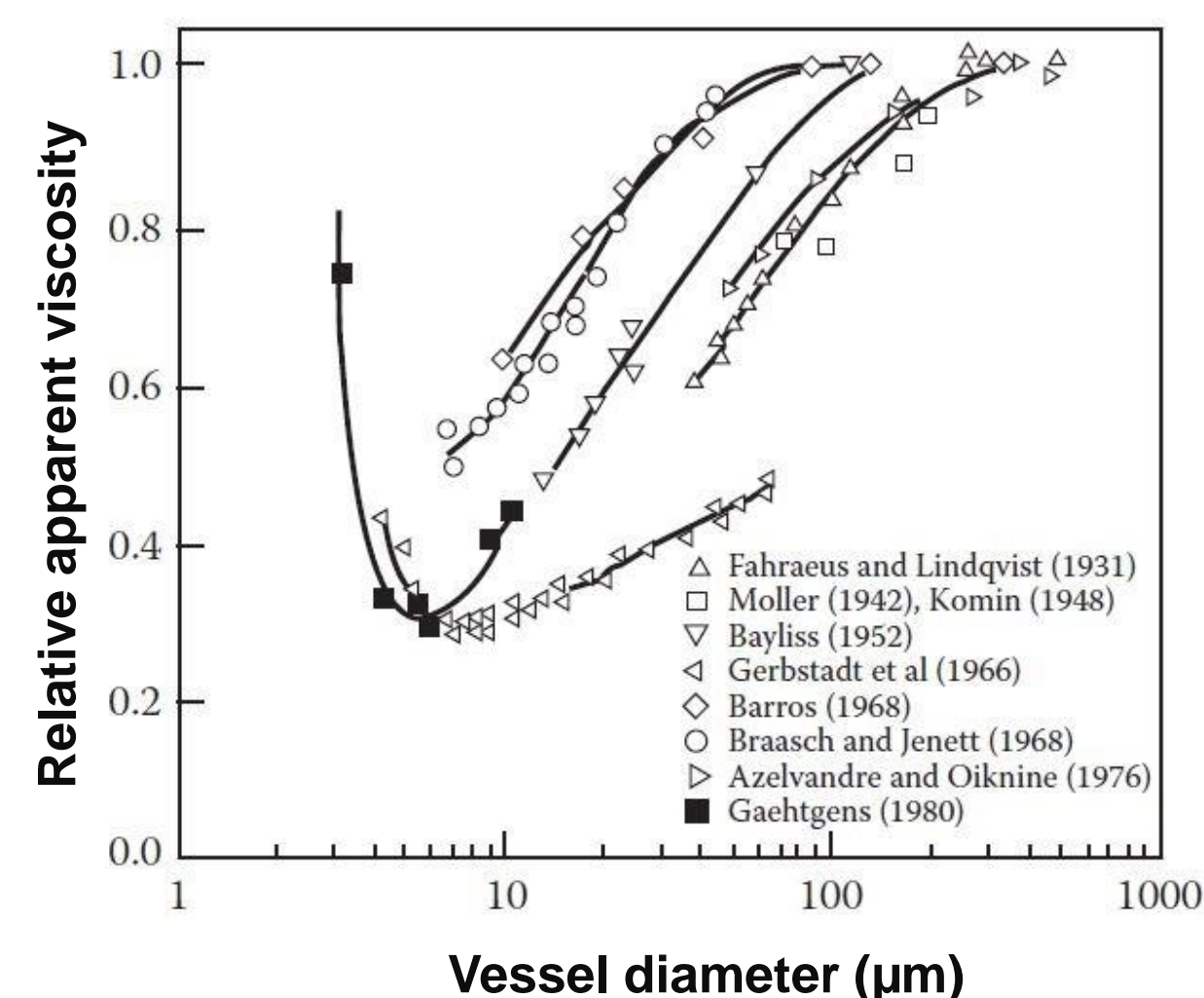


t = 1 h

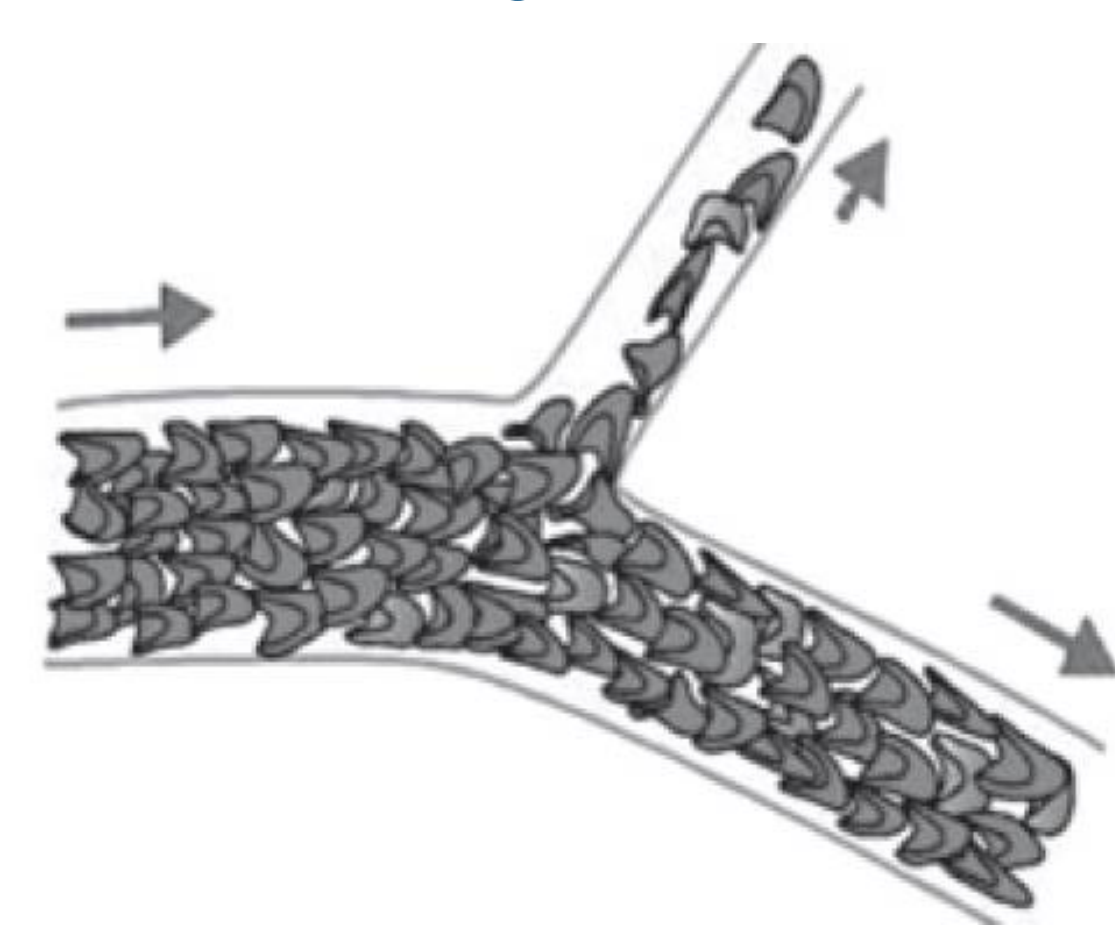
t = 12 h

adapted from: Tiozzo (2017)

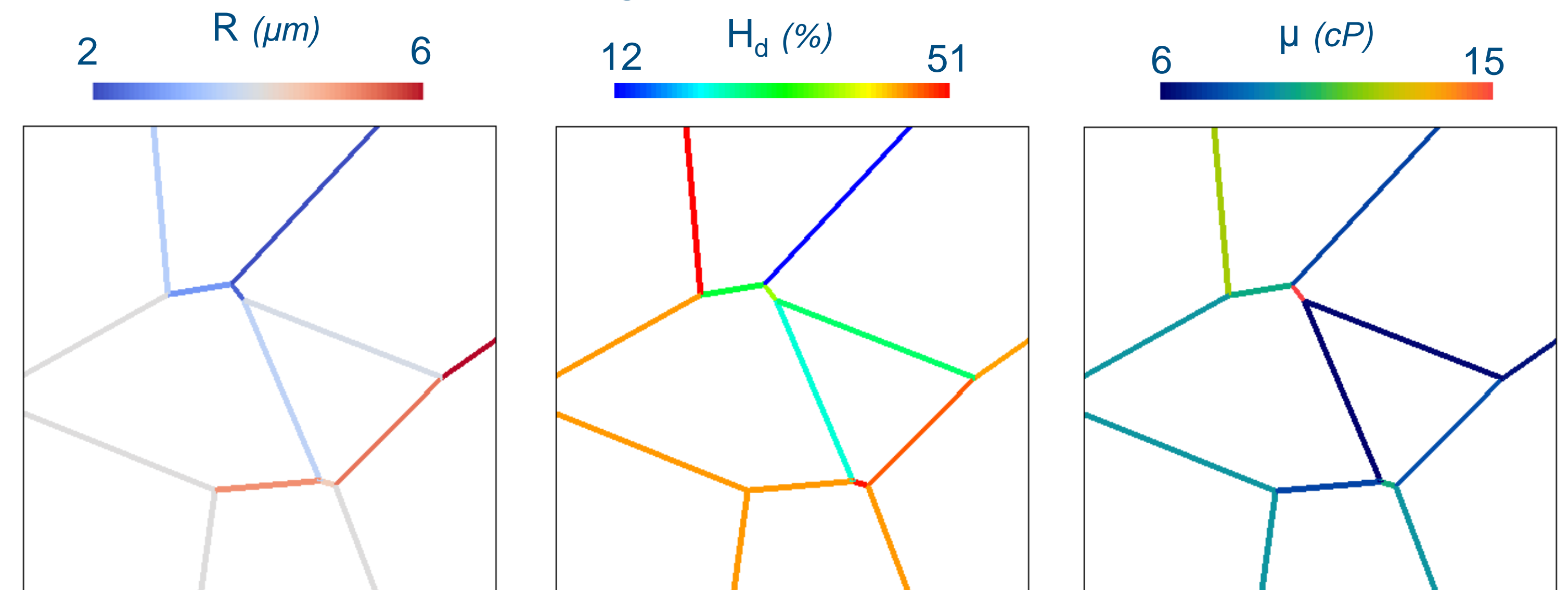
Hematocrit dependent flow properties, including prediction of red blood cells distribution along the vasculature



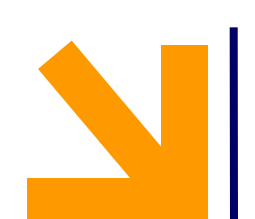
adapted from: Basic Transport Phenomena
in Biomedical Engineering 3/e (2012)



adapted from: Pries et al. (2005)



adapted from: Di Gregorio (2017)



Conclusion and applications

The model can be applied to **compare various treatment options**, such as drug delivery using drug bolus injection and nanoparticles injection into the blood stream. The computational approach is suitable for a **systematic quantification of the treatment performance**, enabling the **analysis of interstitial drug concentration levels, metabolism rates and cell surviving fractions**.



References

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